Computer programs utilized include SHELXS886 (Sheldrick, 1990) for structure solution, SHELX76 (Sheldrick, 1976) for structure refinement, ORTEP (Johnson, 1976) for the preparation of Fig. 1 and SYBYL (Tripos Associates, 1993) for the preparation of Fig. 2.

Lists of structure factors and anisotropic displacement parameters have been deposited with the IUCr (Reference: BR1061). Copies may be obtained through The Managing Editor, International Union of Crystallography, 5 Abbey Square, Chester CHI 2HU, England.

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## Hexagonal $\mathrm{Yb}_{6} \mathrm{Cr}_{4+\mathrm{x}} \mathrm{Al}_{43-\mathrm{x}}(\boldsymbol{x}=\mathbf{1 . 7 6})$ with a New Structure Type

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#### Abstract

The title compound contains one Yb , two Cr and seven Al sites, one of which is about half occupied by Cr . The coordination polyhedron of Yb has the composition $\left[\mathrm{Cr}(\mathrm{Al}, \mathrm{Cr})_{2} \mathrm{Al}_{13} \mathrm{Yb}\right]$, while those around Cr are $\left[\mathrm{Al}_{10} \mathrm{Yb}_{2}\right]$ and $\left[\mathrm{Al}_{12}\right]$, and that around the mixed site is $\left[\mathrm{Al}_{9} \mathrm{Yb}_{3}\right]$.

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## Comment

Aluminium-rich rare-earth $(R)$ transition-metal $(T)$ compounds of approximate composition $R T \mathrm{Al}_{8}$ are known for $R=\mathrm{Y}, \mathrm{Dy}, \mathrm{Sm}, \mathrm{Tb}$ and $T=\mathrm{V}, \mathrm{Cr}$ (Zarechnyuk, Rykhal' \& German, 1971; Rykhal', Zarechnyuk \& Mats'kiv, 1979; Zarechnyuk, Yanson, Ostrovskaya \& Shevchuk, 1988). Investigation of the system Yb-Cr-Al at 773 K revealed the existence of a similar compound.

The structure of $\mathrm{Yb}_{6} \mathrm{Cr}_{4+x} \mathrm{Al}_{43-x}$ is of a new type. It contains one Yb , two Cr and seven Al sites, one of which is occupied partially by Cr (Fig. 1). The coordination polyhedron of Yb has 17 vertices and composition $\left[\mathrm{Cr}(\mathrm{Al}, \mathrm{Cr})_{2} \mathrm{Al}_{13} \mathrm{Yb}\right]$. The polyhedra of the two ordered chromium sites $\mathrm{Cr}(1)$ and $\mathrm{Cr}(2)$, and the disordered metal site $\mathrm{Al}(6)\left(\equiv \mathrm{Al}_{0.56} \mathrm{Cr}_{0.44}\right)$ each have 12 vertices; their compositions are $\left[\mathrm{Al}_{10} \mathrm{Yb}_{2}\right]$, $\left[\mathrm{Al}_{12}\right]$ and $\left[\mathrm{Al}_{9} \mathrm{Yb}_{3}\right]$, respectively. The polyhedra around $\mathrm{Cr}(1)$ and $\mathrm{Al}(6)$ each have a deformed icosahedral shape, while that around $\mathrm{Cr}(2)$ has a regular icosahedral shape, as in many other Al-rich transition-metal compounds (Kripyakevich, 1977). The polyhedra around the other six Al sites all each have 12 vertices and are deformed icosahedra or bicapped pentagonal prisms $[\mathrm{Al}(7)]$. The polyhedra around the $\mathrm{Cr}(1)$ sites are linked parallel to the hexagonal plane in groups of three via common Al atoms and these units are linked perpendicular to the hexagonal plane to form columns along [001] at $x=0, y=0$ via $\mathrm{Cr}(2)$ icosahedra (Fig. 2). Adjacent columns are connected via interpenetrated $\mathrm{Al}(6)$ and Yb polyhedra. All other Al polyhedra interpenetrate with $\mathrm{Cr}(1), \mathrm{Cr}(2)$, $\mathrm{Al}(6)$ or Yb polyhedra. The architecture of the columns of Cr polyhedra (without the Yb atoms) resembles that of hexagonal $\mathrm{V}_{4} \mathrm{Al}_{23}$ (Smith \& Ray, 1957). This structure also contains two transition-metal sites. One of these is icosahedrally coordinated with Al atoms [as is


Fig. 1. Structural projection of hexagonal $\mathrm{Yb}_{6} \mathrm{Cr}_{4+x} \mathrm{Al}_{43-x}$ along [010] showing the coordination polyhedra.


Fig. 2. Coordination polyhedra around $\mathrm{Cr}(1)$ (without the two Yb atoms) and $\mathrm{Cr}(2)$ in $\mathrm{Yb}_{6} \mathrm{Cr}_{4+x} \mathrm{Al}_{43-x}$ viewed along the [001] direction. The $\operatorname{Cr}(2)$ icosahedra are positioned on the plane $z=0$.

(a)

(b)

Fig. 3. Coordination polyhedra around (a) $\mathrm{Cr}(1)$ (without the two Yb atoms) and $\mathrm{Cr}(2)$ in $\mathrm{Yb}_{6} \mathrm{Cr}_{4+x} \mathrm{Al}_{43-x}$ viewed along the [100] direction and (b) around both V sites in $\mathrm{V}_{4} \mathrm{Al}_{23}$ viewed along the [310] direction. $\operatorname{The} \mathrm{Cr}(2)$ and V icosahedra are positioned on the plane $z=0$.
$\mathrm{Cr}(2)$ in the present compound], while the other has eight Al and two V neighbours, thus forming polyhedra which are of the same shape as those of $\mathrm{Cr}(1)$ without the two Yb atoms (Schubert, 1964). These polyhedra are arranged into columns similar to those in $\mathrm{Yb}_{6} \mathrm{Cr}_{4+x} \mathrm{Al}_{43-x}$ at $x=0, y=0$; however, the columns are connected via interpenetrated V -centred $\left[\mathrm{Al}_{8} \mathrm{~V}_{2}\right]$ polyhedra (Fig. 3). The similarity of the stacking in these two compounds is reflected in their cell dimensions, which do not differ much along the hexagonal axes $\left(\mathrm{V}_{4} \mathrm{Al}_{23}: c=17.04 \AA\right)$.

## Experimental

The sample was prepared by arc melting and annealing at 773 K for three weeks.

## Crystal data

$\mathrm{Yb}_{6} \mathrm{Cr}_{5.76} \mathrm{Al}_{41.24}$
$M_{r}=2450.45$
Hexagonal
$\mathrm{P}_{3} / \mathrm{mcm}$
$a=10.867$ (1) $\AA$
$c=17.554$ (2) $\AA$
$V=1795.3(3) \AA^{3}$
$Z=2$
$D_{x}=4.532 \mathrm{Mg} \mathrm{m}^{-3}$

## Data collection

Philips PW1100 diffractometer
$\omega-2 \theta$ scans
Absorption correction:
analytical (LSABS;
Blanc, Schwarzenbach \&
Flack, 1991)
$T_{\text {min }}=0.350, T_{\max }=$ 0.551

3620 measured reflections
980 independent reflections
Mo $K \alpha$ radiation
$\lambda=0.71073 \AA$
Cell parameters from 28 reflections
$\theta=7.5-17^{\circ}$
$\mu=18.148 \mathrm{~mm}^{-1}$
$T=293 \mathrm{~K}$
Needle
$0.064 \times 0.040 \times 0.032 \mathrm{~mm}$
Silver

760 observed reflections

$$
[|F|>3 \sigma(|F|)]
$$

$R_{\text {int }}=0.085$
$\theta_{\text {max }}=29.84^{\circ}$
$h=0 \rightarrow 13$
$k=0 \rightarrow 13$
$l=0 \rightarrow 24$
2 standard reflections frequency: 60 min intensity variations: 1.5 , 1.6\%

## Refinement

Refinement on $F$
$R=0.053$
$w R=0.036$
$S=1.91$
760 reflections
53 parameters
$w=1 / \sigma^{2}(|F|)$
$(\Delta / \sigma)_{\max }=0.0001$
$\Delta \rho_{\text {max }}=7.1 \mathrm{e} \AA^{-3}$
$\Delta \rho_{\text {min }}=-5.0 \mathrm{e}^{-3}$

## Extinction correction:

 Zachariasen (1968)Extinction coefficient: $g=0.06$ (2)
Atomic scattering factors from International Tables for X-ray Crystallography (1974, Vol. IV)

Table 1. Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters ( $\AA^{2}$ )

| $\mathrm{Al}(1)$ | $24(l)$ | $0.2341(4)$ | $0.3952(4)$ | $0.1635(2)$ | $0.009(1)$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{Al}(2)$ | $12(k)$ | $0.1560(5)$ | 0 | $0.1149(3)$ | $0.011(2)$ |
| $\mathrm{Al}(3)$ | $12(k)$ | $0.2529(5)$ | 0 | $0.5289(3)$ | $0.009(2)$ |
| $\mathrm{Al}(4)$ | $12(j)$ | $0.1481(6)$ | $0.5472(6)$ | $1 / 4$ | $0.010(2)$ |
| $\mathrm{Al}(5)$ | $12(i)$ | $0.2495(3)$ | $2 x$ | 0 | $0.029(2)$ |
| $\mathrm{Al}(6) \dagger$ | $8(h)$ | $1 / 3$ | $2 / 3$ | $0.1313(2)$ | $0.010(1)$ |
| $\mathrm{Al}(7)$ | $6(\mathrm{~g})$ | $0.8498(7)$ | 0 | $1 / 4$ | $0.006(2)$ |

$\dagger \mathrm{Al}(6)$ site occupied by 44 (2)\% Cr; set isotropic.

## Table 2. Interatomic distances ( $<4 \AA$ )

| $\mathrm{Yb}-\mathrm{Al}(4)$ | $\times 2$ | 3.044 (6) | $\mathrm{Al}(2)-\mathrm{Al}(7)$ | $\times 2$ | 2.897 (6) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Yb}-\mathrm{Al}(5)$ | $\times 2$ | 3.057 (5) | $\mathrm{Al}(2)-\mathrm{Al}(2)$ | $\times 2$ | 2.936 (7) |
| $\mathrm{Yb}-\mathrm{Al}(1)$ | $\times 2$ | 3.062 (4) | $\mathrm{Al}(2)-\mathrm{Yb}$ |  | 3.389 (4) |
| $\mathrm{Yb}-\mathrm{Al}(3)$ |  | 3.190 (4) | $\mathrm{Al}(2)-\mathrm{Al}(5)$ | $\times 2$ | 3.900 (8) |
| $\mathrm{Yb}-\mathrm{Al}(6)$ | $\times 2$ | 3.219 (1) | $\mathrm{Al}(3)-\mathrm{Al}(2)$ |  | 2.737 (6) |
| $\mathrm{Yb}-\mathrm{Al}(1)$ | $\times 2$ | 3.232 (8) | $\mathrm{Al}(3)-\mathrm{Al}(5)$ | $\times 2$ | 2.740 (9) |
| $\mathrm{Yb}-\mathrm{Al}(3)$ |  | 3.270 (4) | $\mathrm{Al}(3)-\mathrm{Cr}(2)$ |  | 2.795 (8) |
| $\mathrm{Yb}-\mathrm{Al}(5)$ | $\times 2$ | 3.369 (5) | $\mathrm{Al}(3)-\mathrm{Al}(2)$ | $\times 2$ | 2.837 (11) |
| $\mathrm{Yb}-\mathrm{Al}(2)$ |  | 3.389 (4) | $\mathrm{Al}(3)-\mathrm{Al}(1)$ | $\times 2$ | 2.885 (6) |
| $\mathrm{Yb}-\mathrm{Yb}$ |  | 3.444 (1) | $\mathrm{Al}(3)-\mathrm{Al}(3)$ | $\times 2$ | 2.930 (12) |
| $\mathrm{Yb}-\mathrm{Cr}(1)$ |  | 3.498 (2) | $\mathrm{Al}(3)-\mathrm{Yb}$ |  | 3.190 (4) |
| $\mathrm{Cr}(1)-\mathrm{Al}(7)$ | $\times 2$ | 2.478 (4) | $\mathrm{Al}(3)-\mathrm{Yb}$ |  | 3.270 (4) |
| $\mathrm{Cr}(1)-\mathrm{Al}(2)$ | $\times 2$ | 2.638 (5) | $\mathrm{Al}(4)-\mathrm{Cr}(1)$ |  | 2.681 (6) |
| $\mathrm{Cr}(1)-\mathrm{Al}(1)$ | $\times 4$ | 2.681 (8) | $\mathrm{Al}(4)-\mathrm{Al}(1)$ | $\times 2$ | 2.730 (14) |
| $\mathrm{Cr}(1)-\mathrm{Al}(4)$ | $\times 2$ | 2.681 (6) | $\mathrm{Al}(4)-\mathrm{Al}(6)$ | $\times 2$ | 2.732 (12) |
| $\mathrm{Cr}(1)-\mathrm{Yb}$ | $\times 2$ | 3.498 (2) | $\mathrm{Al}(4)-\mathrm{Al}(1)$ | $\times 2$ | 2.764 (6) |
| $\mathrm{Cr}(2)-\mathrm{Al}(2)$ | $\times 6$ | 2.635 (6) | $\mathrm{Al}(4)-\mathrm{Al}(4)$ |  | 2.787 (17) |
| $\mathrm{Cr}(2)-\mathrm{Al}(3)$ | $\times 6$ | 2.795 (8) | $\mathrm{Al}(4)-\mathrm{Yb}$ | $\times 2$ | 3.044 (6) |
| $\mathrm{Al}(1)-\mathrm{Al}(6)$ |  | 2.647 (8) | $\mathrm{Al}(4)-\mathrm{Al}(4)$ | $\times 2$ | 3.062 (24) |
| $\mathrm{Al}(1)-\mathrm{Cr}(1)$ |  | 2.681 (8) | $\mathrm{Al}(5)-\mathrm{Al}(5)$ | $\times 2$ | 2.734 (13) |
| $\mathrm{Al}(1)-\mathrm{Al}(2)$ |  | 2.709 (8) | $\mathrm{Al}(5)-\mathrm{Al}(3)$ | $\times 2$ | 2.740 (9) |
| $\mathrm{Al}(1)-\mathrm{Al}(4)$ |  | 2.730 (14) | $\mathrm{Al}(5)-\mathrm{Al}(6)$ | $\times 2$ | 2.794 (6) |
| $\mathrm{Al}(1)-\mathrm{Al}(4)$ |  | 2.764 (6) | $\mathrm{Al}(5)-\mathrm{Yb}$ | $\times 2$ | 3.057 (5) |
| $\mathrm{Al}(1)-\mathrm{Al}(7)$ |  | 2.792 (9) | $\mathrm{Al}(5)-\mathrm{Al}(1)$ | $\times 2$ | 3.057 (4) |
| $\mathrm{Al}(1)-\mathrm{Al}(3)$ |  | 2.885 (6) | $\mathrm{Al}(5)-\mathrm{Yb}$ | $\times 2$ | 3.369 (5) |
| $\mathrm{Al}(1)-\mathrm{Al}(1)$ |  | 3.032 (7) | $\mathrm{Al}(5)-\mathrm{Al}(2)$ | $\times 2$ | 3.900 (8) |
| $\mathrm{Al}(1)-\mathrm{Al}(1)$ |  | 3.038 (4) | $\mathrm{Al}(6)-\mathrm{Al}(1)$ | $\times 3$ | 2.647 (8) |
| $\mathrm{Al}(1)-\mathrm{Al}(5)$ |  | 3.057 (4) | $\mathrm{Al}(6)-\mathrm{Al}(4)$ | $\times 3$ | 2.732 (12) |
| $\mathrm{Al}(1)-\mathrm{Yb}$ |  | 3.062 (4) | $\mathrm{Al}(6)-\mathrm{Al}(5)$ | $\times 3$ | 2.794 (6) |
| $\mathrm{Al}(1)-\mathrm{Yb}$ |  | 3.232 (8) | $\mathrm{Al}(6)-\mathrm{Yb}$ | $\times 3$ | 3.219 (1) |
| $\mathrm{Al}(2)-\mathrm{Cr}(2)$ |  | 2.635 (6) | $\mathrm{Al}(7)-\mathrm{Cr}(1)$ | $\times 2$ | 2.478 (4) |
| $\mathrm{Al}(2)-\mathrm{Cr}(1)$ |  | 2.638 (5) | $\mathrm{Al}(7)-\mathrm{Al}(1)$ | $\times 4$ | 2.792 (9) |
| $\mathrm{Al}(2)-\mathrm{Al}(1)$ | $\times 2$ | 2.709 (8) | $\mathrm{Al}(7)-\mathrm{Al}(7)$ | $\times 2$ | 2.827 (9) |
| $\mathrm{Al}(2)-\mathrm{Al}(3)$ |  | 2.737 (6) | $\mathrm{Al}(7)-\mathrm{Al}(2)$ | $\times 4$ | 2.897 (6) |
| $\mathrm{Al}(2)-\mathrm{Al}(3)$ | $\times 2$ | 2.837 (11) |  |  |  |

The structure was solved by MULTAN87 (Debaerdemaeker, Germain, Main, Tate \& Woolfson, 1987) and refined by least-squares techniques varying the scale factor, isotropic extinction, atomic positional and anisotropic displacement parameters. The $\mathrm{Al}(6)$ site, about half occupied by Cr , was set isotropic and its occupancy parameter was refined. Xtal3.2 (Hall, Flack \& Stewart, 1992) was used for the data reduction and structure refinement. The high value of the displacement parameter of the $\mathrm{Al}(5)$ site has been noted. Refinement of the occupancy and displacement parameters of the $\mathrm{Al}(5)$ site did not improve the results.

> Lists of structure factors and anisotropic displacement parameters have been deposited with the IUCr (Reference: DU1079). Copies may be obtained through The Managing Editor, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.

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Rietveld Kefinement of the Structures of Dry-Synthesized $M \mathrm{Fe}^{\mathrm{III}} \mathrm{Si}_{2} \mathrm{O}_{6}$ Leucites ( $M=\mathbf{K}, \mathbf{R b}, \mathbf{C s}$ ) by Synchrotron X-ray Powder Diffraction

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## Abstract

Analyses of high-resolution synchrotron X-ray powder diffraction patterns of dry-synthesized $M \mathrm{Fe}^{\text {III }} \mathrm{Si}_{2} \mathrm{O}_{6}$ leucites ( $M=\mathrm{K}, \mathrm{Rb}, \mathrm{Cs}$ ) showed that the K - and Rb containing leucites (iron potassium silicate, $\mathrm{KFeSi}_{2} \mathrm{O}_{6}$, and iron rubidium silicate, $\mathrm{RbFeSi}_{2} \mathrm{O}_{6}$ ) each have a tetragonal $I 4_{1} / a$ structure and the Cs-containing leucite (caesium iron silicate, $\mathrm{CsFeSi}_{2} \mathrm{O}_{6}$ ) has a cubic Ia $\overline{3} d$ structure. The structures of these materials have been refined by the Rietveld method. In $\mathrm{CsFeSi}_{2} \mathrm{O}_{6}$ leucite, $\mathrm{Fe}^{\mathrm{II}}$ and Si are disordered on tetrahedral framework sites as required by space-group constraints. In $\mathrm{KFeSi}_{2} \mathrm{O}_{6}$ leucite, Fe shows significant ordering and is concentrated on the $T_{3}$ tetrahedral site. $\mathrm{RbFeSi}_{2} \mathrm{O}_{6}$ leucite shows less pronounced $T$-site ordering reflecting the fact that it is closer to the tetragonal-cubic phase transition at which the $T$ sites become identical.

